

## Syllabus Course description

| Course title      | Operations Research                               |
|-------------------|---|
| Course code       | 42150   |
| Scientific sector | MAT/09  |
| Degree            | Bachelor in Industrial and Mechanical Engineering |
| Semester          | II  |
| Year              | II  |
| Academic Year     | 2017-2018   |
| Credits           | 6   |
| Modular           | No  |

| Total lecturing hours | 36                       |
|-----------------------|--------------------------|
| Total lab hours       |                          |
| Total exercise hours  | 24                       |
| Attendance            | Recommended              |
| Prerequisites         | Basics of Linear Algebra |
| Course page           |                          |

| -                    |  |  |  |  |  |
|----------------------|--|--|--|--|--|
|                      | The course aims to present the main quantitative methods used to support economic and technical decisions. |  |  |  |  |
|                      | In addition to the traditional themes of Operations  |  |  |  |  |
|                      | Research, such as Linear Programming and Network   |  |  |  |  |
| Specific educational | Problems, the course develops some alternative and   |  |  |  |  |
| objectives           | original approaches, such as Game Theory.  |  |  |  |  |
|                      | The goal is to provide the student with an independent   |  |  |  |  |
|                      | capability to examine a real problem involving decision-   |  |  |  |  |
|                      | making, to formulate a mathematical model for  |  |  |  |  |
|                      | representing it, to develop a suitable algorithm to achieve  |  |  |  |  |
|                      | a solution and, finally, to interpret the results.   |  |  |  |  |

| Lecturer                             | Prof. GianDemetrio Marangoni  |  |  |  |
|--------------------------------------|---|--|--|--|
| Scientific sector of the<br>lecturer | SECS-P/01   |  |  |  |
| Teaching language                    | English   |  |  |  |
| Office hours                         | 18  |  |  |  |
| Teaching assistant (if any )         | -   |  |  |  |
| Office hours                         | -   |  |  |  |
| List of topics covered               | Foundation of Matrix Algebra and Linear Systems<br>Matrices and vectors - Linear combination of vectors -<br>Determinants - Inverse matrix - Linear systems -<br>Solution methods<br>Linear Programming<br>Linear Programming problems - Maximisation problems -<br>The fundamental theorem of Linear Programming - The<br>simplex method - Minimisation problems - The auxiliary<br>problem - Sensitivity analysis - Shadow prices - The |  |  |  |

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|                 | theory of duality   |  |  |  |
|-----------------|---|--|--|--|
|                 | Integer linear programming  |  |  |  |
|                 | Continuous and integer linear programming - The cuttin plane method - The branch and bound method - Binar   |  |  |  |
|                 |   |  |  |  |
|                 | programming   |  |  |  |
|                 | Graph Theory  |  |  |  |
|                 | Graphs and networks - Matrix representation of a graph -  |  |  |  |
|                 | The shortest spanning tree - Shortest path - Maximum  |  |  |  |
|                 | flow problems   |  |  |  |
|                 | Input-Output Analysis   |  |  |  |
|                 | Origins and applications of the input-output model - The  |  |  |  |
|                 | input-output quantity model - The input-output price  |  |  |  |
|                 | model - The Leontief inverse - Impact analysis and  |  |  |  |
|                 | production multipliers  |  |  |  |
|                 | Game Theory   |  |  |  |
|                 | Static games - Discrete and continuous strategies -   |  |  |  |
|                 | Iterated elimination of strictly dominated strategies - Nash  |  |  |  |
|                 | equilibrium with discrete strategies - Nash equilibrium   |  |  |  |
|                 | with continuous strategies - Mixed strategies - Dynamic   |  |  |  |
|                 | games - The game tree and backward induction -  |  |  |  |
|                 | Subgame-perfect Nash equilibrium - Backward induction   |  |  |  |
|                 | and subgame-perfect Nash equilibrium - Dynamic games  |  |  |  |
|                 |   |  |  |  |
|                 | Foundations of Differential Calculus  |  |  |  |
|                 | Mavima and minima for functions of 1 variable. Mavima   |  |  |  |
|                 | Maxima and minima for functions of 1 variable - Maxima  |  |  |  |
|                 | Maxima and minima for functions of 1 variable - Maxima<br>and minima for functions of 2 or more variables –   |  |  |  |
| Tooching format | Maxima and minima for functions of 1 variable - Maxima<br>and minima for functions of 2 or more variables –<br>Constrained maxima and minima  |  |  |  |
| Teaching format | Maxima and minima for functions of 1 variable - Maxima<br>and minima for functions of 2 or more variables –<br>Constrained maxima and minima<br>Lectures, exercises and computer lab  |  |  |  |
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|   | Formative and Summative assessment   |     |                     |                  |  |
|---|--|-----|---------------------|------------------|--|
|   | During the course, one or more tests will be held to verify<br>the achievement of the teaching objectives by the<br>students.<br>The tests will be discussed upon the occasion of the final<br>exam. |     |                     |                  |  |
| Assessment  | Form   | %   | Length<br>/duration | ILOs<br>assessed |  |
|   | Written exam<br>and oral<br>discussion:<br>theory and<br>exercises   | 70% | 2 hours             | 1-5              |  |
|   | Computer lab:<br>exercises   | 30% | 1 hour              | 1-5              |  |
| Assessment language                                 | English  |     |                     |                  |  |
| Evaluation criteria and criteria for awarding marks | Knowledge of theoretical basis, correctness in applying<br>solution techniques, correctness of results, ability to set<br>up and solve a problem with Excel software                                 |     |                     |                  |  |
| Required readings                                   | GianDemetrio Marangoni, Mathematical Programming and<br>Economic Analysis, Lugano, Università della Svizzera<br>italiana, 2018   |     |                     |                  |  |
| Supplementary readings                              | Hillier, Liberman, Introduction to Operations Research, 10 <sup>th</sup> ed., McGrawHill, 2015   |     |                     |                  |  |